

## 140A-Introduction to Solid State Physics--Study guide for first midterm:

### Coverage:

Don't worry about memorizing complicated formulas, just try to understand their origin and how to use them. The exam will have a table of pertinent equations and constants on its first page. If needed, I will hand out a sheet with the 14 Bravais lattices.

### •Reading-

- Omar: All of Chapter 1, plus Sections 5.1-5.3 to p. 181, not Energy Bands, 5.8 through Eq. 5.28 only; 2.1-2.7
- For anyone in need of a review of basic quantum mechanics, Omar has a nice review in Appendices A.1-A.3, A.5, A.7, and A.8, which total only 10 pages
- Ibach and Luth: All of Chapter 1, 2.1-2.5 only, but lighter on 2.2 and 2.4, all lecture slides, through Slide 19 in Slide Set 3, all problems assigned to date

### Some concepts to understand or questions to be able to answer:

#### •Course introduction:

- How is solid state physics/condensed matter physics important in fundamental science (e.g. Nobel Prizes in Physics, nanoscience) and modern technology (e.g. Moore's Law, magnetic data storage, energy production)?
- What is a field effect transistor? Why is it important?
- What is a nanostructure? Why are they important?

#### •Review of some basic quantum mechanics and atomic physics: (Largely from Ibach and Luth, but see Appendices A.1-A.3, A.5 in Omar if needed)

- Review of the hydrogen atom problem in quantum mechanics; separation into radial, polar, and azimuthal parts of wave function  $\psi$ ; extension to many-electron atoms via a screened Coulomb interaction and  $Z_{\text{eff}}$
- Conversion of imaginary atomic wave functions into real form for use in linear combination of atomic orbitals (LCAO) = tight-binding (TB) description of covalent bonding
- Many-electron wave functions for Fermions, anti-symmetry and the Pauli Principle
- Anti-symmetry and the Fermi hole for spin-parallel electrons, giving rise to the exchange interaction and lower energies if more electrons have parallel spin, thus also magnetism and Hund's First Rule.
- Filling of the periodic table, including reasoning for order of filling subshells: 1s, 2s, 2p, 3s, 3p, 4s, 3d, ..., and special cases when outer d or f shells are half-, or totally-filled

#### •Bonding in molecules and solids: (Largely Ibach and Luth, but see Omar, Appendices A.7, and A.8 if needed)

#### •Cohesive energy (lattice energy) of a crystal: meaning and calculation, including from individual bond energies in covalent solids

#### •Covalent bonding:

- Simple quantum-mechanical description of bonding in a diatomic molecule via LCAO (tight-binding) description, minimization of energy, meaning of  $H_{AA}$ ,  $H_{BB}$ ,  $H_{AB}$ ,  $H_{BA}$ ,  $S_{AA}$ ,  $S_{BB}$ ,  $S_{AB}$ ,  $S_{BA}$ , origin of secular equation for solution
- For simple molecules: bonding and anti-bonding wave functions, sigma and pi character
- Filling of molecular electronic levels
- Energy as a function of interatomic distance for molecules and solids: contributions from electron-nuclear attraction, nuclear-nuclear repulsion, and electron-electron repulsion
- Directed bonds:  $sp^3$  tetrahedral bonding,  $sp^2+p$  bonding, other possibilities with d orbitals
- Broadening of electronic states into bands for solids, filling of bands and solid types based on filling: metallic, ferromagnetic metallic, insulator, semiconductor, ionic solid

#### •Metallic bonding:

- Some valence electrons acting essentially like free electrons, delocalize to reduce their energy and screen the core-core repulsions left behind
- Transition metals (3d, 4d, 5d and 4f, 5f series) have mixture of covalent and metallic bonding, example of Cu  $3d^{10}(covalent)4s^1(metallic, free-electron like)$

#### •Ionic bonding:

- Ionization potential and electron affinity
- Electronegativity as measure of net electron attracting power
- Calculation of the net ionic attraction with  $1/r$  variation and the Madelung constant

- Repulsive potential at short distance due to electron-electron repulsion with  $1/r^n$  variation
- Calculation of binding energy (lattice energy) of crystal; derivation of pertinent parameters from form of overall interaction
- Van der Waals attraction:
  - Oscillating dipoles due to electrons on atoms:  $1/r^6$  variation
- Hydrogen bonding:
  - H atom bound to very electronegative atom → weak bond to another electronegative atom
- Relative strengths of five interaction types: covalent, metallic, ionic, van der Waals, hydrogen bonding
  - Bloch functions for electrons in periodic potential, general properties

•Crystal structures: Primarily from Omar, Chapter 1

- Translational periodicity and translation symmetry operations: meaning
- Basis vectors and the Bravais lattice
- Bravais lattice + basis = crystal
- Recognition of the Bravais lattice and the basis in a real crystal
- Unit cells: primitive and non-primitive
- Primitive and non-primitive basis vectors for a given structure
- 14 types of three dimensional Bravais lattices
- Planes in crystals and Miller indices: (hkl) and sets {hkl}
- Directions in crystals: [hkl] and sets <hkl>.
- Spacings between planes in crystals with orthogonal basis vectors
- Formulas of compounds from the crystal structure; counting atoms in the unit cell
- Packing of touching spheres in different crystals
- Other special crystal structures: sodium chloride, cesium chloride, diamond
- Calculation of ideal ionic radii ratios in different ionic crystals: cesium chloride, sodium chloride, zinc blende
- Point group symmetry operations:
  - Rotations by  $2\pi/n = n$ -fold rotation
  - Reflection in a mirror plane
  - Inversion ( $\vec{r} \rightarrow -\vec{r}$ )
- Crystal group = Translation group + Point group

•Diffraction and Crystal Structure Determinations-“Lite”: Primarily Chapter 2 in Omar, but less quantitative for midterm, dealing only with problem types assigned in Problem Set 2 and simpler questions on scattering and diffraction

- Types of scattering and diffracting de Broglie waves: photon, electron, neutron, helium atom,...
- Generation of x-rays: x-ray tube, synchrotron radiation
- Bragg's Law: two views via planar reflection and scattering from an array of individual atoms
- Derivation of the scattered intensity, basic formulas, division into atomic scattering factor  $f_a$ , geometric (unit cell or basis) structure factor F and lattice structure factor S
- The atomic scattering factor; general form and derivation
- The reciprocal lattice and its vectors  $G_{hkl}$ .
- The Ewald construction
- Forbidden reflections for some crystal structures (e.g., bcc and fcc) due to F
- Brillouin zones